

$$f(x) \quad (10, 16)$$
$$f^{-1}(x) \quad (16, 10)$$

$$f^{-1}(x) \quad (3, -16)$$

$$m = \frac{-16 - 10}{3 - 16} = \frac{-26}{-13} = \textcircled{m=2}$$

$$-16 = 2(3) + b$$

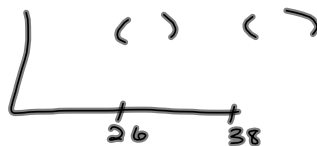
$$\begin{array}{r} -16 \\ -6 \\ \hline \end{array} = \frac{6}{6} + b$$

$$\textcircled{-22 = b}$$

$$f^{-1}(x) = 2x - 22$$

$$\begin{aligned} 28. \quad f(x) &= x + 4 \\ y &= x + 4 \\ x &= y + 4 \\ x - 4 &= y \\ f^{-1}(x) &= \boxed{y = x - 4} \end{aligned}$$

36. $(26, 37.79)$
 $(38, 41.39)$



$$\frac{41.39 - 37.79}{38 - 26} = \frac{3.60}{12} = \$0.30 \text{ per minute}$$

$$m = 0.3$$

$$37.79 = 0.3(26) + b$$

$$37.79 = 7.80 + b$$

$$\begin{array}{r} -7.80 \\ \hline \end{array}$$

$$\$29.99 = b$$

a)

$$y = 0.3x + \$29.99$$

$$c(x) = 0.3x + 29.99$$

b) $c^{-1}(x) =$

$$x = 0.3y + 29.99$$

$$\begin{array}{r} x - 29.99 = 0.3y \\ \hline 0.3 \end{array}$$

$$\boxed{\frac{x - 29.99}{0.3} = y}$$

c) the additional minutes used

d) $y = 0.3x + 29.99$

$$48.89 = 0.3x + 29.99$$

$$\begin{array}{r} -29.99 \\ \hline \end{array}$$

$$\frac{18.90}{0.3} = \frac{0.3x}{0.3}$$

$$63 = x$$

63 additional minutes

4-7 Inverse functions

(x, y) inverse (y, x)

$(4, -10)$ $(-10, 4)$

$f(x)$

$f^{-1}(x)$

Inverse function

- 1.) replace $f(x)$ with y
- 2.) interchange the x and the y
- 3.) solve for y
- 4.) replace (rewrite) the equation
 $f^{-1}(x)$

$$f(x) = 4x - 8 \quad \text{1. rewrite the function}$$

$$y = 4x - 8 \quad \text{2.) } y = x$$

$$x = 4y - 8 \quad \text{3.) change the } x \text{ and } y$$

$$\begin{array}{r} +8 \\ x = 4y - 8 \end{array}$$

$$\frac{x + 8}{4} = \frac{4y}{4}$$

$$\frac{1}{4}x + 2 = y$$

4.) solve for x

5.) rewrite as the inverse function

$$y = \frac{1}{4}x + 2$$

$$\boxed{f^{-1}(x) = \frac{1}{4}x + 2}$$

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22)

$$3y - 12x = -72$$

$$\frac{3}{3}y = \frac{12}{3}x - \frac{72}{3}$$

$$y = 4x - 24$$

original equation in
slope intercept form

$$x = 4y - 24$$

replace x and y

$$\frac{x}{4} + \frac{24}{4} = \frac{4}{4}y$$

solve for y

$$\frac{1}{4}x + 6 = y$$

rewrite as the inverse

$$\boxed{f^{-1}(x) = \frac{1}{4}x + 6}$$